- **1.** Given $f(x) = \sin x + 2\cos x$, $-\frac{\pi}{4} \le x \le 0$, find $(f^{-1})'(a)$ for a = 2.
- **2.** Solve for x:
- (a). $e^{3x-7}=6$

(b). $\ln(x+1) - \ln x = 1$

- **3.** Given $f(x) = \ln(\cos x + 2)$
- (a). What is the domain of f?
- (b). Find the relative extreme $\underline{\text{values}}$ on the interval [-1,1].

[Indicate max or min.]

4. Evaluate the following integrals.

(a).
$$\int_0^1 \frac{1}{4-2x} dx$$

(f).
$$\int \operatorname{sech}^2(5x) dx$$

(b).
$$\int e^{-7x} - \frac{7 \ln x}{x} dx$$

(g).
$$\int \sec(5x) \ dx$$

(c).
$$\int \frac{3x^2 + 2x}{x^3 + x^2 + 1} \, dx$$

(h).
$$\int_0^{\ln 2} \frac{e^{3x} + 1}{e^x} \, dx$$

$$(\mathbf{d}). \int \frac{3x}{\sqrt{1-36x^2}} \, dx$$

(e).
$$\int \frac{3}{\sqrt{1-36x^2}} dx$$

(i).
$$\int \frac{\tan x}{\ln(\cos x)} dx$$

- **5.** Given the function $f(x) = e^{-x^2}$
- (a). Evaluate $\lim_{x \to -\infty} e^{-x^2}$
- **(b).** Evaluate $\lim_{x \to +\infty} e^{-x^2}$
- (c). Find f'(x)
- **6.** What is the formula for $\log_a x$ in terms of the natural logarithmic function?
- 7. Find the exact value of
- (a). $\sin(2\tan^{-1}(1))$

- **(b).** $\cos^{-1}\left(\cos\left(\frac{7\pi}{6}\right)\right)$
- **8.** Simplify the following expression so that it is an algebraic expression of x:
- $\cos(\sin^{-1}(2x))$

9. Differentiate the following functions:

(a).
$$y = x^4 - 4^x + e^{4x} + \ln 4x$$

(d).
$$h(\theta) = 3\ln\left(\frac{2+\cos\theta}{\theta^2}\right)$$

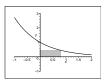
(b).
$$y = x^{\frac{1}{x}}$$

(e).
$$y = \cosh(\ln(x^3 + 2x^2))$$

(c).
$$y = \pi^x - \ln e^x$$

(f).
$$f(x) = x \sin^{-1}(3x)$$

- **10.** Find the equation of the tangent line to $y = \log_3 x$ at x = 1
- 11. (a). Find the maximum area of a rectangle in the first quadrant with 2 sides on the x- and y-axes and one vertex on the curve $y = e^{-x}$. See the figure below. [Hint: Express the area of such a rectangle in terms of x only.]



- (b). Sketch the picture for a rectangle in the first quadrant with 2 sides on the x- and y-axes and one vertex on the curve $y = e^x$. Without using Calculus, determine whether there exists such a rectangle with a maximum area. Briefly explain (a couple of sentences) why or why not.
- 12. Given that a population follows the law of exponential growth, $y(t) = Ce^{kt}$ where y is the population and t is time in years.
- (a). Find the proportional constant k, if the population triples every 50 years.
- (b). If the population is 100 after 5 years, find the population at time t.
- 13. Find the following limits. You must clearly show all steps and indicate where you use L'Hopital's Rule.

(a).
$$\lim_{x\to 0} \frac{\sin 4x}{2x}$$

(b).
$$\lim_{x \to \infty} (1+x)^{\frac{1}{x}}$$

(c).
$$\lim_{x\to 2} \frac{x-2}{x^2-3x+2}$$

(a).
$$\lim_{x\to 0} \frac{\sin 4x}{2x}$$
 (b). $\lim_{x\to \infty} (1+x)^{\frac{1}{x}}$ (c). $\lim_{x\to 2} \frac{x-2}{x^2-3x+2}$ (d). $\lim_{x\to 2} \frac{x-2}{x^2-3x-2}$