

- No calculators, books, or notes (in any form) allowed.
- Clearly indicate your answers.
- **Show all your work** – partial credit may be given for written work.
- Evaluate trigonometric, exponential, and logarithmic expressions for standard values.
- Good Luck!

Formulas that you may or may not find helpful

$$\sin^2 \theta = \frac{1}{2} - \frac{1}{2} \cos 2\theta$$

$$\cos^2 \theta = \frac{1}{2} + \frac{1}{2} \cos 2\theta$$

$$\sin 2\theta = 2 \sin \theta \cos \theta$$

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta = 1 - 2 \sin^2 \theta = 2 \cos^2 \theta - 1$$

$$\sin A \cos B = \frac{1}{2} [\sin(A+B) + \sin(A-B)] = \frac{1}{2} \sin(A+B) + \frac{1}{2} \sin(A-B)$$

$$\cos A \cos B = \frac{1}{2} [\cos(A+B) + \cos(A-B)] = \frac{1}{2} \cos(A+B) + \frac{1}{2} \cos(A-B)$$

$$\sin A \sin B = \frac{1}{2} [\cos(A-B) - \cos(A+B)] = \frac{1}{2} \cos(A-B) - \frac{1}{2} \cos(A+B)$$

$$\sin(-\theta) = -\sin \theta$$

$$\cos(-\theta) = \cos \theta$$

$$\int \sec \theta \, d\theta = \ln |\sec \theta + \tan \theta|$$

$$\int \csc \theta \, d\theta = \ln |\csc \theta - \cot \theta|$$

Score	
1	/8
2	/24
3	/8
4	/24
5	/20
6	/12
7	/4
8	/4
Total	/100

1. (8 pts). Write down the **form only** of the partial fraction decomposition for the following fraction.

[Do **NOT** determine the values of the coefficients.]

[Note: $x^2 + x + 1$ does not factor.]

$$\frac{x^3 + 2x^2 - 5}{x(3-x)^3(x^2+x+1)^2}$$

2. (24 pts). Evaluate the following integrals.

(a). $\int e^x \sin(4x) dx$

(b). $\int \sqrt{\cos x} \sin^3 x dx$

(c). $\int_{1/2}^{e/2} \ln(2x) dx$ [Simplify your answer.]

3. (8 pts). Use The Trapezoid Rule with $n = 5$ to approximate the integral $\int_0^1 \sqrt{1+x^3} dx$. Do not simplify!!

4. (24 pts). Evaluate the following integrals.

(a). $\int \frac{-3x + 8}{x(x - 2)^2} dx$

(b). $\int \frac{1}{x\sqrt{x^2 + 16}} dx$

5. (20 pts). Evaluate the following integrals or show that it is a divergent improper integral

(a). $\int_0^2 \frac{1}{1-x} dx$

(b). $\int_{-\infty}^0 xe^x dx$

6. (12 pts). Determine whether the following sequences converge or diverge. **If it converges, find the limit.** **If it diverges, clearly explain the reason why.** [Clearly indicate $+\infty$ or $-\infty$ in the case of an infinite limit.]

(a). $a_n = \frac{3(-1)^n}{n}$

(b). $b_n = \sqrt{\frac{4n-3}{1+9n}}$

7. (4 pts). List out the first 4 terms of the following sequence.

$$a_1 = 6, \quad a_{n+1} = \frac{a_n}{n}$$

8. (4 pts). *True or False.* Determine whether the following statements are true or false.

T F If $f(x) \leq g(x)$ and $\int_0^\infty g(x) dx$ diverges, then $\int_0^\infty f(x) dx$ also diverges.

T F $\int \sin^2(2x) dx = \int \frac{1}{2} - \frac{1}{2} \cos(2x) dx$