

Practice differentiating the following with respect to t .

1.

(a). If x does not depend on t (i.e. x is constant), then

$$\frac{d}{dt}[x] = 0$$

(b). If x depends on t , then

$$\frac{d}{dt}[x] = \frac{dx}{dt}$$

2.

(a). If y does not depend on t (i.e. y is constant), then

$$\frac{d}{dt}[y^2] = 0$$

(b). If y depends on t , then

$$\frac{d}{dt}[y^2] = 2y \frac{dy}{dt}$$

3.

(a). If x does not depend on t (i.e. x is constant) and y depends on t , then

$$\frac{d}{dt}[x^2 + y^2] = 2y \frac{dy}{dt}$$

(b). If x depends on t and y does not depend on t (i.e. y is constant), then

$$\frac{d}{dt}[x^2 + y^2] = 2x \frac{dx}{dt}$$

(c). If x depends on t and y depends on t , then

$$\frac{d}{dt}[x^2 + y^2] = 2x \frac{dx}{dt} + 2y \frac{dy}{dt}$$

4.

(a). If x does not depend on t (i.e. x is constant) and y depends on t , then

$$\frac{d}{dt}[xy] = x \frac{dy}{dt}$$

(b). If x depends on t and y does not depend on t (i.e. y is constant), then

$$\frac{d}{dt}[xy] = y \frac{dx}{dt}$$

(c). If x depends on t and y depends on t , then

$$\frac{d}{dt}[xy] = x \frac{dy}{dt} + y \frac{dx}{dt}$$

5.

(a). If x does not depend on t (i.e. x is constant), then $\frac{d}{dt} [\sin x] = 0$

(b). If x depends on t , then $\frac{d}{dt} [\sin x] = \cos x \frac{dx}{dt}$

6.

(a). If x does not depend on t (i.e. x is constant) and y depends on t , then $\frac{d}{dt} \left[\frac{x}{y} \right] = \frac{-x}{y^2} \frac{dy}{dt}$

(b). If x depends on t and y does not depend on t (i.e. y is constant), then $\frac{d}{dt} \left[\frac{x}{y} \right] = \frac{1}{y} \frac{dx}{dt}$

(c). If x depends on t and y depends on t , then $\frac{d}{dt} \left[\frac{x}{y} \right] = \frac{y \frac{dx}{dt} - x \frac{dy}{dt}}{y^2}$

7.

(a). If r does not depend on t (i.e. r is constant) and h depends on t , then $\frac{d}{dt} \left[\frac{1}{3} \pi r^2 h \right] = \frac{1}{3} \pi r^2 \cdot \frac{dh}{dt}$

(b). If r depends on t and h does not depend on t (i.e. h is constant), then $\frac{d}{dt} \left[\frac{1}{3} \pi r^2 h \right] = \frac{1}{3} \pi h \cdot 2r \frac{dr}{dt}$

(c). If r depends on t and h depends on t , then $\frac{d}{dt} \left[\frac{1}{3} \pi r^2 h \right] = \frac{1}{3} \pi r^2 \cdot \frac{dh}{dt} + h \left(\frac{1}{3} \pi \cdot 2r \frac{dr}{dt} \right)$