

1. Given the following information, find the values of the remaining trigonometric functions.

$$\tan \theta = 3, \quad \pi < \theta < \frac{3\pi}{2}.$$

2. Solve the following equations for x .

(a). $2\sin^2 x - \sqrt{2}\sin x = 0$ (x in $[0, 2\pi]$)

(b). $\cos \frac{x}{2} = 0$ (x in $[0, 2\pi]$)

3. Given $\theta = \frac{3\pi}{4}$, find $\sin 2\theta$.

4. Differentiate the following using **Differentiation Rules**.

(a). $s(t) = (3t^3 - t^2 + 7)^{23}$

(b). $f(\theta) = \theta \sin(\theta^2 + 1)$

(c). $y = \frac{x(2x^4 + 4)^8}{\tan 2x}$ [Do not simplify!]

5. Find the equation of the tangent line to the curve $y = \sqrt[3]{2x^2 - 5}$ at $x = 4$.

6. Given $f(x) = g(3x^2)$, find f' in terms of g' .

7. If a stone is thrown vertically upward on the moon with a velocity of 8 m/s, its height after t seconds is given by $y = 8t - 0.83t^2$, [Calculator*]

(a). What is the velocity after 2 s?

(b). What is the velocity at impact?

8. A tank holds 1000 gallons of water, which drains from the bottom of the tank in 50 minutes. Torricelli's Law gives the volume V of water remaining in the tank after t minutes as $V = 1000 \left(1 - \frac{1}{50}t\right)^2$ for $0 \leq t \leq 50$. Find the rate at which the water is draining from the tank after 10 minutes. Include units in your answer.

9. The cost function for a certain commodity is $C(x) = 60 + 0.12x - 0.0004x^2 + .000002x^3$. [Calculator*]

(a). Find the marginal cost function.

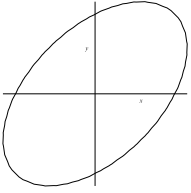
(b). Find and interpret $C'(50)$.

(c). Compare $C'(50)$ with the cost of producing the 51st item.

10. Any Section 2.7 applications.

*Similar non-calculator problems could be given.

11. Given the curve drawn below and defined by $x^2 + y^2 = 3 + xy$
- (a). Find $\frac{dy}{dx}$
- (b). On the graph below, sketch any tangents lines to the curve where the slope is 0.
- (c). Use part (a) to find these points on the curve where the slope is 0. Must show work for credit.
- (d). Find $\frac{d^2y}{dx^2}$ in terms of x and y .



12. Given $f(x) = \sqrt{x} = x^{1/2}$
- (a). Find the linearization $L(x)$ at $a = 25$
- (b). Use this linearization $L(x)$ to approximate $\sqrt{24.7}$ [Simplify your answer.]
- (c). Find the differential dy for x going from 25 to 25.5.
13. A ladder 8 feet long is leaning against the wall of a house. On the ground, the base of the ladder is being pulled away from the wall at a rate of $\frac{3}{2}$ ft/sec. How fast is the angle between the top of the ladder and the wall changing when this angle is $\frac{\pi}{3}$.
14. A particle moves along the curve $xy^2 = 12$. As it reaches the point $(3, 2)$, the y -coordinate is decreasing at a rate of 2 cm/s. How fast is the x -coordinate of the particle position changing at that instant?
15. Find the critical numbers for $g(t) = 4t^3 - 3t^2 + 1$
16. Given $f(x) = 2\sqrt{x} - x$, find the absolute maximum and minimum values of $f(x)$ on the interval $[0, 9]$.
17. Given $f(x) = \frac{(x-1)^3}{x^2}$
- (a). Find the intervals of increase or decrease.
- (b). Find the local maximum and minimum values.
- (c). Find the intervals of concavity and the inflection points.

18. Given $f(\theta) = \cos^2(\theta)$, on $0 \leq \theta \leq 2\pi$,

- (a). Find the intervals of increase or decrease.
- (b). Find the local maximum and minimum values.
- (c). Find the intervals of concavity and the inflection points.

19. Section 3.3 #27