

Name: Key

Math 151-02 Calculus I - Crawford

Quiz 3-B

24 October 2017

Books, notes (in any form), and calculators are not allowed. *Show all your work.* Good Luck!

1. (4 pts) Find the critical numbers of the function.

$$f(t) = (t^2 - 16)^3$$

$$f'(t) = 3(t^2 - 16)^2 \cdot 2t = 0$$

$$6t(t^2 - 16)^2 = 0$$

$$6t = 0 \quad \text{or} \quad t^2 - 16 = 0$$

$t = 0$	$t^2 = 16$
	$t = \pm 4$

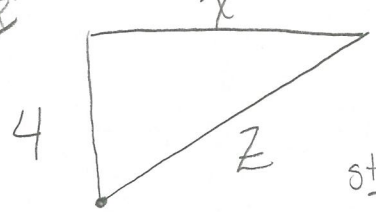
(Note: $f'(t)$ exists everywhere)

2. (4 pts) Turn in Section 2.8, #15 by 3pm today. If you turn it in immediately after turning in this quiz, I'll give you 2 bonus points.

See Back for 2017

3. (7 pts) A plane flying horizontally at an altitude of 4 mi and a speed of 500 mi/h passes directly over a radar station. Find the rate at which the distance from the plane to the station is increasing when the plane has flown horizontally 3 miles.

[Remember that significant partial credit will be given for clearly and accurately labeling the picture, and indicating values and equations in correct mathematical notation.]

Step 1 

Step 2 x = distance plane flies $\frac{dx}{dt}$ = velocity of plane
 z = distance between plane & radar station $\frac{dz}{dt}$ = rate dist. between changes

Step 3 Find $\frac{dz}{dt}$ when $x = 3$ mi
 $\frac{dx}{dt} = 500$ mi/h

Step 4 $x^2 + 4^2 = z^2$

Steps $\frac{d}{dt}[x^2 + 4^2] = \frac{d}{dt}[z^2]$
 $2x \frac{dx}{dt} = 2z \frac{dz}{dt}$
 $\frac{x}{z} \frac{dx}{dt} = \frac{dz}{dt}$

Still need z at the same instant.
 $3^2 + 4^2 = z^2$
 $9 + 16 = z^2$
 $25 = z^2$
 $z = 5$

Now subs.

Step 6 $\frac{3}{5} \cdot 500 = \frac{dz}{dt} \Rightarrow \boxed{\frac{dz}{dt} = 300 \text{ mi/h}}$

Section 2.8 #15

Step 2 x = dist. man is from pole $\frac{dx}{dt}$ = velocity of man
 z = dist. tip of shadow from pole $\frac{dz}{dt}$ = rate the tip of shadow moves

Step 3 Find $\frac{dz}{dt}$ when $x = 40$ ft
 $\frac{dx}{dt} = 5$ ft/s

Step 4 Similar triangles

$$\frac{z}{15} = \frac{z-x}{6} \Rightarrow \frac{z}{15} = \frac{z-x}{6} \cdot \frac{5}{5} \Rightarrow 2z = (z-x)5$$

$$2z = 5z - 5x \Rightarrow 5x = 3z \leftarrow \text{simplified}$$

Step 5 $\frac{d}{dt}[5x] = \frac{d}{dt}[3z]$ **Step 6** $5(5) = 3 \frac{dz}{dt}$

$$5 \frac{dx}{dt} = 3 \frac{dz}{dt} \Rightarrow \boxed{\frac{dz}{dt} = \frac{25}{3} \text{ ft/s}}$$