

TRANSLATIONS

For $c > 0$, the following translations shift the original graph $y = f(x)$ as indicated.

<u>Translation</u>	<u>Shift</u>	<u>Example</u>	<u>Graph</u>
$y = f(x) + c$		$y = x^2 + 2$	
$y = f(x) - c$		$y = x^2 - 3$	
$y = f(x - c)$		$y = (x - 4)^2$	
$y = f(x + c)$		$y = (x + 1)^2$	

Ex: Sketch $y = \sqrt{x + 2} + 3$

REFLECTIONS

$$y = f(-x)$$

$$y = -f(x)$$

$$y = |f(x)|$$

Ex: Sketch $y = |x^3 + 1|$

Ex: Sketch $y = \frac{-1}{x-1}$

DILATIONS

For $c > 0$, the following dilations stretch or compress the original graph $y = f(x)$ as indicated.

For $c > 1$, _____ the graph of $y = f(x)$ _____ by a factor of c
 $y = cf(x)$

For $0 < c < 1$, _____ the graph of $y = f(x)$ _____ by a factor of c

For $c > 1$, _____ the graph of $y = f(x)$ _____ by a factor of $\frac{1}{c} < 1$
 $y = f(cx)$

For $0 < c < 1$, _____ the graph of $y = f(x)$ _____ by a factor of $\frac{1}{c} > 1$

Ex: Given the following graph of $y = f(x)$,

Sketch

(a). $y = 2f(x)$

(c). $y = f(4x)$

(b). $y = \frac{1}{3}f(x)$

(d). $y = f\left(\frac{1}{2}x\right)$