Finish proof of |ab| = |a||b| (cases 2 & 4). Cases 1 & 3 done in class.

Section 3, p. 19: #5, 6, 7, 8 [See hints below.]

<u>#3.5(a)</u> This proof justifies taking off absolute values, [e.g. |x - 3| < 4 can be written as -4 < x - 3 < 4.] Remember it is an if and only if problem, so you must prove both "If A, then B" (\Rightarrow :) and "If B, then A" (\Leftarrow :).

 \Rightarrow : Show $-a \leq b$ and $b \leq a$ separately.

 $\Leftarrow: \text{Use } 2 \text{ cases: } b \ge 0 \text{ and } b < 0.$

#3.5(b) If you can show $-|a-b| \le |a| - |b| \le |a-b|$, then you can use part (a). Show $-|a-b| \le |a| - |b|$ and $\overline{|a| - |b|} \le |a-b|$ separately.

#3.6 How do you mathematically make 3 (or more) things into 2 things?

#3.8 [I am introducing a part(a) to prove first which will help to prove the original question.]

(a) Prove: Let $a, b \in \mathbb{R}$. If a > b, then $b_1^* = b + \frac{1}{2}|a - b|$ is between b and a [i.e. $b < b_1^* < a$].

Before you prove part(a), draw a number line with $a, b, and b_1^*$. From this picture, describe specifically how the point b_1^* is related to a and b.

(b) Use contradiction (and at some point, part (a)) to prove the original #3.8:

Let $a, b \in \mathbb{R}$. Show that if $a \leq b_1 \quad \forall b_1 > b$, then $a \leq b$.