Ex: [Chemical Equations] Liquid benzene $\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)$ burns in the atmosphere $\left(\mathrm{O}_{2}\right)$. If a cold object is placed over the benzene, a reaction occurs that results in water $\left(\mathrm{H}_{2} \mathrm{O}\right)$ and soot, i.e. Carbon (C), forming on the object. The unbalanced chemical equation is given by

$$
\mathrm{C}_{6} \mathrm{H}_{6}+\mathrm{O}_{2} \longrightarrow \mathrm{C}+\mathrm{H}_{2} \mathrm{O}
$$

Since the atoms are neither created nor destroyed, the equation must be balanced by finding $x_{1}, x_{2}, x_{3}$, and $x_{4}$ such that the total $\mathrm{C}, \mathrm{H}$, and O atoms on the LHS match the total on the RHS. i.e.

$$
x_{1} \mathrm{C}_{6} \mathrm{H}_{6}+x_{2} \mathrm{O}_{2} \longrightarrow x_{3} \mathrm{C}+x_{4} \mathrm{H}_{2} \mathrm{O}
$$

Ex: [Traffic Flow] Construction causes the following traffic network (with one-way traffic). Determine the general flow for the network.


Ex: [Economics] A primitive society currently barters 3 main goods: Food, Tools, and Clothing. The farmers keep $50 \%$ of the food themselves and give (i.e. trade) $30 \%$ to tool producers and $20 \%$ to clothing producers. The tool producers keep $30 \%$ of tools and give $35 \%$ to both food and clothing producers. The clothing manufacturers keep $40 \%$ of clothing and give $40 \%$ to the food producers and $20 \%$ to the tool producers.

The data can be summarized in the following or Graphically

## Exchange Table:

| Food | Tools | Clothing | Traded To |
| :---: | :---: | :---: | :---: |
|  |  | Food |  |
|  |  | Tools |  |
|  |  |  |  |
|  |  |  |  |

Now the society wants to introduce a monetary system and they want to know how to price the goods so that each group's expenses balances its income (i.e. $\qquad$ ).

Let
$x_{1}=$ price of food
$x_{2}=$ price of tools
$x_{3}=$ price of clothing

In order to be in equilibrium: Total Income $=$ Total Expense

|  | Total Income | $=$ | Total Expenses on |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Food | Tools | Clothing |
| Food | $x_{1}$ | $=$ |  |  |
| Tools | $x_{2}$ | $=$ |  |  |
| Clothing | $x_{3}$ | $=$ |  |  |

