

A matrix with only one column is called a _____ and denoted $\mathbf{u} = \begin{bmatrix} u_1 \\ u_2 \\ \vdots \\ u_n \end{bmatrix}$

EX:

The entries can be written as _____ called an n -tuple.

EX:

_____ is the set of all n -tuples where each entry is in _____ .

EX: $n = 2$: (u_1, u_2) is an _____ and defines a point in _____ .

EX: $n = 3$: (u_1, u_2, u_3) is an _____ and defines a point in _____ .

Graphical Representations of vectors in \mathbb{R}^2 and \mathbb{R}^3 .

$\mathbf{u} = \begin{bmatrix} a \\ b \end{bmatrix}$ can be represented by a line segment w/ an arrow from the origin to the point (a, b) . But

Addition of two vectors: Add corresponding entries $\mathbf{u} + \mathbf{v} = \begin{bmatrix} u_1 \\ u_2 \\ \vdots \\ u_n \end{bmatrix} + \begin{bmatrix} v_1 \\ v_2 \\ \vdots \\ v_n \end{bmatrix} =$

Examples and Graphical Representations

Scalar Multiplication ($c \in \mathbb{R}$ is a scalar): Multiply each element by c . $c\mathbf{u} = c \begin{bmatrix} u_1 \\ u_2 \\ \vdots \\ u_n \end{bmatrix} =$

Examples and Graphical Representations

Properties for vectors \mathbf{u}, \mathbf{v} , and \mathbf{w} in \mathbb{R}^n and scalars $c, d \in \mathbb{R}$.

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|--|---|
| 1. $\mathbf{u} + \mathbf{v} = \mathbf{v} + \mathbf{u}$ | 5. $c(\mathbf{u} + \mathbf{v}) = c\mathbf{u} + c\mathbf{v}$ |
| 2. $(\mathbf{u} + \mathbf{v}) + \mathbf{w} = \mathbf{u} + (\mathbf{v} + \mathbf{w})$ | 6. $(c + d)\mathbf{u} = c\mathbf{u} + d\mathbf{u}$ |
| 3. $\mathbf{u} + \mathbf{0} = \mathbf{0} + \mathbf{u} = \mathbf{u}$ | 7. $c(d\mathbf{u}) = (cd)\mathbf{u}$ |
| 4. $\mathbf{u} + (-\mathbf{u}) = -\mathbf{u} + \mathbf{u} = \mathbf{0}$ | 8. $1\mathbf{u} = \mathbf{u}$ |