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Section 2.1 Example

$$\frac{dy}{dt} - 2ty = 1$$

General solution: $y(t) = e^{t^2} \left(\int_0^t e^{-s^2} ds \right) + C e^{t^2}$

> ysoln := (t) -> exp(t^2) * int(exp(-s^2), s = 0 .. t) + 3 * exp(t^2);

$$ysoln := t \mapsto e^{t^2} \left(\int_0^t e^{-s^2} ds \right) + 3 e^{t^2} \quad (1)$$

Let's have Maple compute $y(2)$:

> ysoln(2);

$$\frac{e^4 \operatorname{erf}(2) \sqrt{\pi}}{2} + 3 e^4 \quad (2)$$

Note that the answer is in terms of the error function, which is defined as $\operatorname{erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$

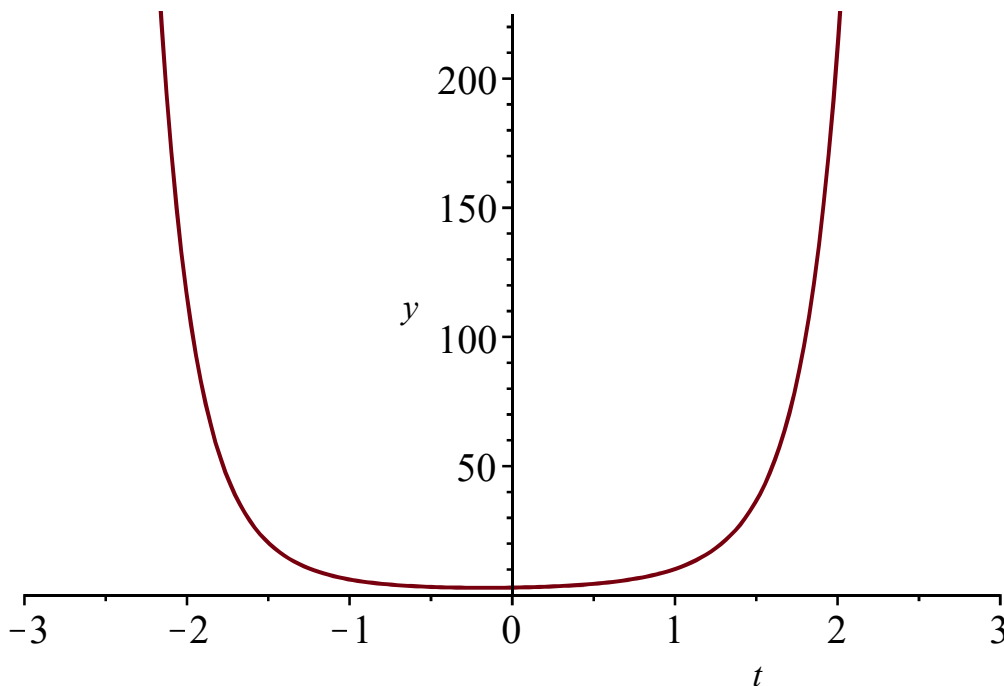
The error function is well-known and Maple can evaluate it, so a decimal approximation for $y(2)$ is:

> evalf(ysoln(2));

$$211.9544622 \quad (3)$$

Maple can also plot curves involving integrals with a variable for one of the bounds:

> plot(ysoln(t), t=-3..3, y=0..225);



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Just for reference, here's a plot of the error function,  $f(x) = \text{erf}(x)$ :
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> plot(erf(x), x=-3..3);
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