

```
> restart;
```

### Section 2.1 Example

$$\frac{dy}{dt} - 2ty = 1$$

General solution:  $y(t) = e^{2t} \left( \int_0^t e^{-s^2} ds \right) + C e^{t^2}$

```
> ysoln := (t) -> exp(t^2) * int(exp(-s^2), s = 0 .. t) + 3 * exp(t^2);
```

$$ysoln := t \rightarrow e^{t^2} \left( \int_0^t e^{-s^2} ds \right) + 3 e^{t^2} \quad (1)$$

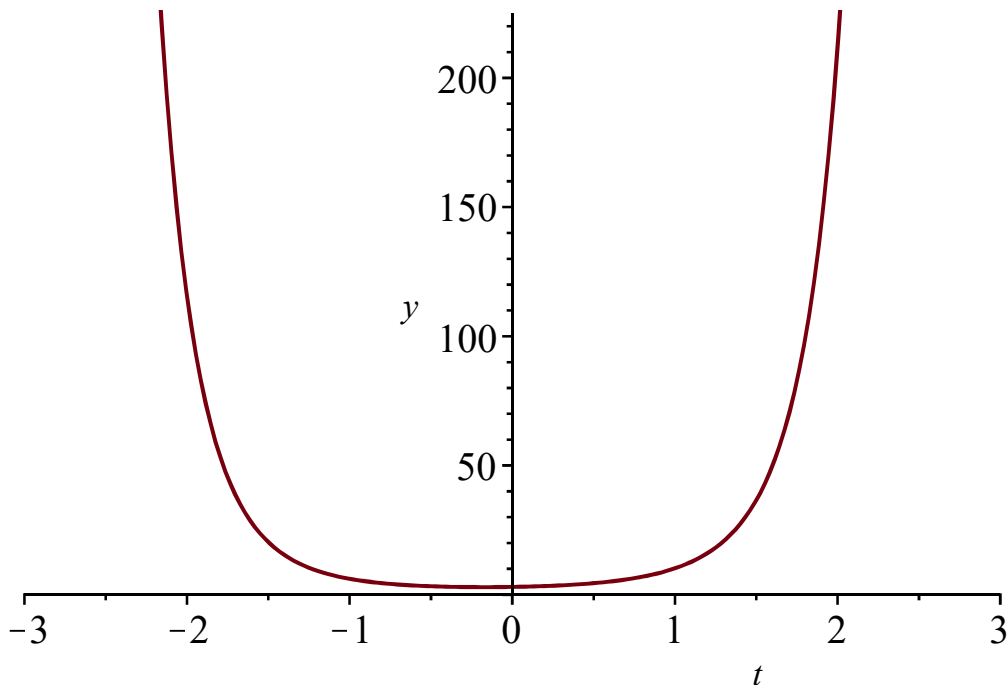
Let's have Maple compute y(2):

```
> ysoln(2);
```

$$\frac{1}{2} e^4 \operatorname{erf}(2) \sqrt{\pi} + 3 e^4 \quad (2)$$

Maple can also plot curves involving integrals with a variable for one of the bounds:

```
> plot(ysoln(t), t = -3..3, y = 0..225);
```



Note that the answer is in terms of the error function, which is defined as  $\operatorname{erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$

The error function is well-known and Maple can evaluate it:

```
> evalf(ysoln(2));
```

$$211.9544622 \quad (3)$$

```
>
```

Just for reference, here's a plot of the error function, erf(x):

```
> plot(erf(x), x=-3..3);
```

