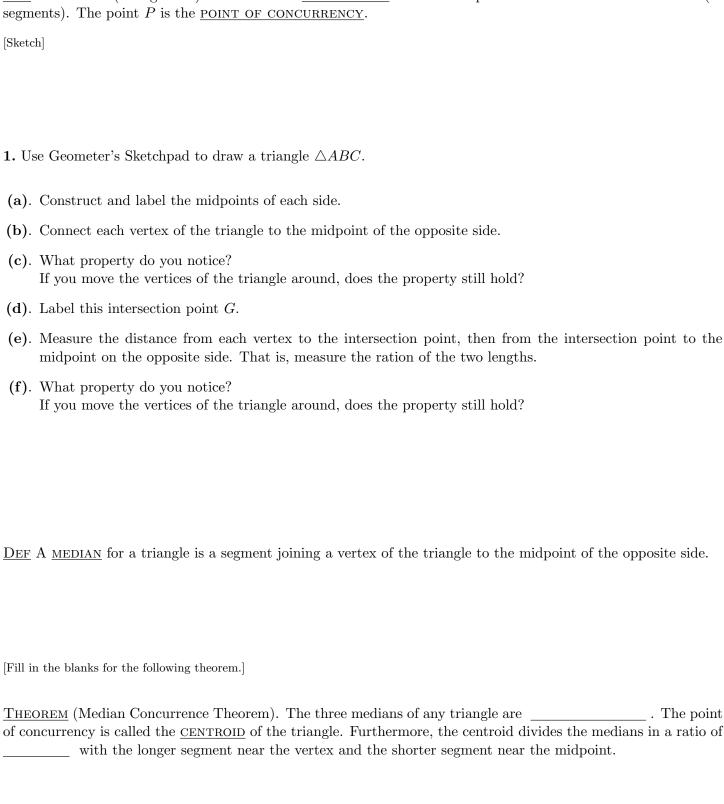
Triangle Centers

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DEF Three lines (or segments) are said to be CONCURRENT if there is a point P that lies on all three lines (or segments). The point P is the POINT OF CONCURRENCY.



[In GSP, label the centroid G and hide the medians.]

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2. <u>Def</u> An altitude for a triangle is a line through one vertex that is perpendicular to the line determined by the opposite two vertices.
(a). Using the already constructed triangle, construct the three altitudes. What property do you notice?
(b). Does the property hold or change for acute or obtuse triangles?
[Fill in the blanks for the following theorem.]
<u>Theorem</u> (Altitude Concurrence Theorem). The three altitudes of any triangle are The point of concurrency is called the <u>ORTHOCENTER</u> of the triangle.
[In GSP, label the orthocenter H and hide the altitudes.]
3. (a). Using the already constructed triangle, construct the three perpendicular bisectors. What properties do you notice? Are there any properties about the distances?
(b). Do these property hold or change for acute or obtuse triangles?
[Fill in the blanks for the following theorem.]
<u>Theorem</u> (Perpendicular Bisector Concurrence Theorem). The three perpendicular bisectors of any triangle are The point of concurrency is called the <u>CIRCUMCENTER</u> of the triangle. Furthermore, the distances from the circumcenter to each vertex are
[In GSP, label the circumcenter O and hide the perpendicular bisectors.]
4. Move the vertices of the triangle around.
(a). What property do you notice about the three centers G, H , and O ?
(b). Measure the distances HG and GO . Then calculate HG/GO . Move the vertices around to see what property holds.
[Fill in the blanks for the following theorem.]
THEOREM (Euler Line Theorem). The centroid G , the circumcenter O , and the orthocenter H of any triangle are This common line is called the <u>EULER LINE</u> . Furthermore, if the triangle is not equilateral, G is between H and G an
What happens if the triangle is equilateral?