AXIOMS OF NEUTRAL GEOMETRY

- 1. The Existence Postulate
- 2. The Incidence Postulate
- 3. The Ruler Postulate
- 4. The Plane Separation Postulate
- **5**. The Protractor Postulate
- **6**. The Side-Angle-Side Postulate

Add the Euclidean Parallel Postulate and we finally get to Euclidean Geometry.

AXIOM 7 EUCLIDEAN PARALLEL POSTULATE For every line l and for every point P that does not lie on l, there is exactly one line m such that P lies on m and $m \parallel l$.

Prove each of the following in Euclidean Geometry.

[Note: They are not true in Neutral or Hyperbolic Geometry.]

1. <u>Converse to the Alternate Interior Angles Theorem</u>: If two parallel lines are cut by a transversal then both pairs of alternating interior angles are congruent.

Sketch a diagram.

Hint: Use proof by contradiction.

Proof



