

DEF A triangle is a _____ triangle if one of the interior angles is a right angle. The side opposite the right angle is called the _____ and the two sides adjacent to the right angle are called the _____.

THEOREM (Hypotenuse-Leg Theorem) Let $\triangle ABC$ and $\triangle DEF$ be two right triangles with right angles at C and F . If $\overline{AB} \cong \overline{DE}$ and $\overline{BC} \cong \overline{EF}$, then $\triangle ABC \cong \triangle DEF$.

Sketch a diagram for this theorem. Continue to add to the picture as you prove the theorem.

PROOF Let $\triangle ABC$ and $\triangle DEF$ be two right triangles with right angles at C and F .

Let $\overline{AB} \cong \overline{DE}$ and $\overline{BC} \cong \overline{EF}$, [Show $\triangle ABC \cong \triangle DEF$.]

Let G be a point on \overrightarrow{AC} such that $\overline{CG} \cong \overline{FD}$ (Point Construction Postulate).

Then $\angle BCG$ forms a _____ with $\angle BCA$.

Thus by the Linear Pair Theorem, $\mu(\angle BCG) = \underline{\hspace{2cm}}$.

So $\triangle BCG \cong \triangle EFD$ by _____.

Since these two triangles are congruent, _____ $\cong \overline{DE}$.

Therefore $\overline{GB} \cong \underline{\hspace{2cm}}$ from the given statements.

Hence $\triangle ABG$ is an _____ triangle.

Thus _____ by the Isosceles Triangle Theorem.

Therefore $\triangle ABC \cong \triangle DEF$. by _____ . ■

Go back to the given statements. What type of triangle congruence is this theorem? (e.g. SAS, ASA, etc.)

So in the special case of _____ triangles, _____ congruency holds.

See the board for diagrams of SSA possibilities and sketch them below.

From the picture, fill in the blanks to the theorem. [Hint for the second blank: Look at the diagram with both options for the placement of point B , call them B and B' . What type of triangle is $\triangle BCB'$?]

THEOREM (Side-Side-Angle (SSA)): If $\triangle ABC$ and $\triangle DEF$ are triangles such that $\angle BAC \cong \angle EDF$, $\overline{AC} \cong \overline{DF}$, and $\overline{BC} \cong \overline{EF}$, then $\triangle ABC$ _____ $\triangle DEF$ or $\angle ABC$ and $\angle DEF$ are _____.

PROOF Let $\triangle ABC$ and $\triangle DEF$ be triangles such that $\angle BAC \cong \angle EDF$, $\overline{AC} \cong \overline{DF}$, and $\overline{BC} \cong \overline{EF}$.

By the Point-Construction Postulate, choose a point G on \overrightarrow{AB} such that $AG = DE$.

Case 1: $G = B$.

[Finish this case.]

Case 2: $G \neq B$. Then $A * G * B$ or $A * B * G$. WLOG assume $A * G * B$ otherwise we could restart the proof interchanging $\triangle ABC$ and $\triangle DEF$.

[Finish the proof.]

So far, we've been sketching our pictures by making the known angle acute. Do you get the same possible triangles if the known angle is obtuse?