Name: _

Math 331 Foundations of Geometry – Crawford

Books and notes (in any form) are not allowed. You may use the provided list of Axioms, Postulates, and Theorems. **Show all your work**. Partial credit may be given for written work. GOOD LUCK!

1. (18 pts) Given $\triangle ABC$, let D be a point such that B * D * C and AC = DC. Also let $\mu(\angle CAD) = 32^{\circ}$.

(b). Fill in the blank or explain why there is not enough information to determine: $\mu(\angle ACD) =$ _____.

(c). True or False or Not Enough Information to Determine:

(a). Fill in the blank or explain why there is not enough information to determine:

(d). True of False of Not Enough Information to Determine:

19 November 2015

Exam 2

CB > AC.

AB > AC.

 $\mu(\angle ADB) = \underline{\qquad}.$

(a). If $\triangle ABC$ and $\triangle DEF$ are triangles such that $\angle BAC \cong \angle EDF$, $\overline{AC} \cong \overline{DF}$, and $\overline{BC} \cong \overline{EF}$, then $\triangle ABC \cong \triangle DEF$.

(b). If $\Box ABCD$ is a quadrilateral such that AB = AD and CB = CD, then $\Box ABCD$ is a convex quadrilateral.

(c). Let $\triangle XYZ$ be an equilateral triangle. Let P, Q, and R be points such that Y * X * P, X * Z * Q, and Z * Y * R and XP = ZQ = YR. Then $\triangle PQR$ is equilateral.

(d). The angle bisector of $\angle BAC$ intersects \overline{BC} at its midpoint.

3. (6 pts) Determine whether the following statements are TRUE or FALSE. [No sketch or explanation necessary.]

- (a). In a model for Neutral Geometry: Given a line l_0 and an external point P_0 , if there exists a line *m* through P_0 such that $m \parallel l_0$, then the Euclidean Parallel Postulate must hold.
- (b). If $\mu(\angle ACB) = \mu(\angle ABC)$, then AB = AC.
- (c). If AB + BC = AC, then A, B, and C are collinear.
- 4. (12 pts) Fill in the blanks to prove Property 4 of Lambert Quadrilaterals (Theorem 4.8.11, part 4).

<u>PROOF</u> : Let $\Box ABCD$ be a Lambert quadrilatera	l with right angles at	vertices A, B , and C .	[Show $BC \leq AD$.]
---	------------------------	-----------------------------	-----------------------

BWOC, suppose

Then by point construction, construct a point E between B and C such that BE =_____.

Then $\Box ABED$ is a _____ quadrilateral by definition.

Then $\mu(\angle BED) \le 90^{\circ}$ by _____

But $\angle BED$ is an _____ to $\triangle ECD$.

Therefore $\mu(\angle BED) >$ by the Exterior Angle Theorem.

This is a contradiction $(\rightarrow \leftarrow)$ to

Therefore, _____

5. (24 pts) Prove 2 of the following. Clearly state theorems and properties that you use.

<u>BONUS</u>: You may do (or attempt) all three options and each will be graded out of 12 points. Whichever two you score higher on will be your base grade. Any points from the third problem will be cut in third and added to your base grade.

- (a). (Old) Use the Hinge Theorem to prove THEOREM 4.2.7 (SSS): If $\triangle ABC$ and $\triangle DEF$ are two triangles such that $\overline{AB} \cong \overline{DE}, \overline{BC} \cong \overline{EF}$ and $\overline{CA} \cong \overline{FD}$, then $\triangle ABC \cong \triangle DEF$.
- (b). (Old) Prove LEMMA 4.5.3 (Two-Angles Sum): If $\triangle ABC$ is any triangle, then $\mu(\angle CAB) + \mu(\angle ABC) < 180^{\circ}$.
- (c). (New) Prove the following corollary to the Alternate Interior Angles Theorem: If l and l' are lines cut by a transversal t in such a way that two nonalternating interior angles on the same side of t are supplements, then l is parallel to l'.

6. (24 pts) The take-home portion of the exam is due Saturday, November 21 by 10am. If you do not turn it in to me in person by Friday, November 21 at 3pm, you may scan it and email it to me. It must be a pdf file, not jpg, and make sure it is legible before sending. The public computer lab in Daniels Hall has scanners that you can use.