

Name: _____

Math 251 Calculus III – Crawford

Quiz 2

01 March 2016

Books, notes (in any form), and calculators are not allowed. *Show all your work.* Good Luck!

1. (4 pts) Reduce the following equation to one of the standard forms and classify the surface.
[ellipsoid, cone, elliptic paraboloid, hyperboloid of one sheet, hyperboloid of two sheets, hyperbolic paraboloid].

$$x^2 + 4x - y^2 - 4z^2 + 4 = 0$$

2. (5 pts) Find the limit, if it exists. If it does not exist, clearly indicate the reason why.

[Simplify.]

$$\lim_{t \rightarrow 0} \left\langle 3e^{-4t}, \cos(2t), \frac{\sin(5t)}{t} \right\rangle$$

3. (6 pts) Find a parametric equation for the tangent line to the curve with the given parametric equations at the specified point.

$$x = t^2 + 3, \quad y = 2\sqrt{t}, \quad z = \ln(t^2); \quad (4, 2, 0)$$

4. (5 pts) Evaluate the following integral for the two-dimensional vector-valued function.

$$\int 2t^3 \mathbf{i} + \sin(2t) \mathbf{j} \, dt$$