

1. Given the vector $\mathbf{v} = \langle 2, 3, -4 \rangle$
 - (a). Find a unit vector in the same direction as \mathbf{v}
 - (b). Find a vector in the opposite direction as \mathbf{v} that has a magnitude of 3.

2. Determine whether the the vectors $\mathbf{u} = \mathbf{i} - \mathbf{j} + 2\mathbf{k}$ and $\mathbf{v} = 4\mathbf{i} - 2\mathbf{j} + 2\mathbf{k}$ are orthogonal, parallel, or neither.

3. Show that the following equation represents a sphere and find its center and radius.
 $x^2 + y^2 + z^2 - 2x + 6y + 8z + 1 = 0$

4. Given the points $P(1, 0, 1)$, $Q(1, -1, 4)$, and $R(3, -1, 1)$,
 - (a). Find a vector orthogonal to the plane through the points P , Q , and R .
 - (b). Find the area of the triangle PQR .

5. A constant force is given by the vector $F = 3\mathbf{i} + 4\mathbf{j} + 5\mathbf{k}$ and moves an object along a straight line from the points $P(2,1,0)$ and $Q(3,5,2)$. Find the work done.

6. Describe in your own words the vector and scalar projections of \mathbf{b} onto \mathbf{a} . Use a sketch if necessary.

7. Given $\mathbf{u} = \langle 1, 2, 4 \rangle$, $\mathbf{v} = \langle 2, -1, 2 \rangle$, and $\mathbf{w} = \langle 1, 0, -1 \rangle$,
 - (a). Are the three vectors coplanar?
 - (b). If not, find the scalar and vector projections of \mathbf{u} onto \mathbf{w} .

8. Given the point $(2, 2, 1)$ and the line $x = 2t, y = 4 + 2t, z = t$,
 - (a). Find the equation of a plane that passes through the point and contains the line.
 - (b). Find the symmetric equations of a line passing through $(2, 2, 1)$ and perpendicular to the plane found in part (a).

9. Given the two planes $5x - 3y + z = 4$ and $x + 4y + 7z = 1$
 - (a). Determine whether they are parallel, perpendicular, or neither.
 - (b). If they are parallel, find the distance between them. If they are neither, find the cosine of the angle between them.

10. Reduce the equation $4x^2 - y^2 - 2z^2 + 12z = 18$ to one of the standard forms, classify the surface, and describe (or sketch) it.

11. Section 12.6, p. 857 #21-28 (matching)

12. Find the domain of the vector function $\left\langle \frac{t}{3t-1}, e^{1/t}, \cos(t) \right\rangle$

13. Evaluate the following limits.
 - (a). $\lim_{t \rightarrow \infty} \left\langle e^{-t}, \frac{1}{t}, \frac{t^2}{t^2+1} \right\rangle$
 - (b). $\lim_{t \rightarrow 2} \left(t\mathbf{i} + \frac{t^2-4}{t^2-2t}\mathbf{j} + \frac{1}{t}\mathbf{k} \right)$

14. Section 13.1, p. 870: #21-26 (matching)

15. Sketch the plane curve given by the vector equation $\mathbf{r}(t) = 3\mathbf{i} - t\mathbf{j} + t^2\mathbf{k}$. Indicate with an arrow the direction in which t increases.

16. Find a vector function that represents the curve of intersection of the paraboloid $z = x^2 - y^2$ and the cylinder $x^2 + y^2 = 1$.

17. Given the space curve with the parametric representation $x = 9 \cos t$, $y = 9 \sin t$, and $z = e^t$,

(a). Sketch the curve and indicate with an arrow the direction of increasing t .

(b). Find the tangent vector when $t = \frac{\pi}{2}$ and sketch it on the curve.

18. Evaluate the following integrals:

(a). $\int_1^e \frac{1}{t} \mathbf{i} + t\mathbf{j} + \frac{1}{t^2} \mathbf{k} dt$

(b). $\int \frac{t}{1+t^2} \mathbf{i} + \cos 2t\mathbf{j} + \sqrt{t}\mathbf{k} dt$

19. Find $\mathbf{r}(t)$ if $\mathbf{r}'(t) = t\mathbf{i} - e^{2t}\mathbf{j}$ and $\mathbf{r}(0) = \mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$.

20. Given the curve represented by position vector $\mathbf{r}(t) = \langle 5t^2 - t, 3t, \sin \pi t \rangle$

(a). Find the unit tangent vector at $P(4, 3, 0)$.

(b). Find the equation of the tangent line to the curve at the same point $P(4, 3, 0)$.

21. Given the position vector $\mathbf{r}(t) = \langle \cos 2t, 0, \sin 2t \rangle$,

(a). Find the length of the curve for $\pi/2 \leq t \leq \pi$.

(b). Find the unit tangent, normal, and binormal vectors $\mathbf{T}(t)$, $\mathbf{N}(t)$, and $\mathbf{B}(t)$.

(c). Use the formula $\kappa(t) = \frac{|\mathbf{T}'(t)|}{|\mathbf{r}'(t)|}$ to find the curvature.

22. Given the vector equation $\mathbf{r}(t) = \langle 1 + 6t, 3 - 2t, 3t \rangle$ for a curve

(a). Find the arc length function measured from $P(1, 3, 0)$ [i.e. $t=0$] in the direction of increasing t .

23. The acceleration of a particle is given by the vector $\mathbf{a}(t) = \mathbf{k}$. Find the velocity vector $\mathbf{v}(t)$ and position vector $\mathbf{r}(t)$ if the initial velocity and position vectors are $\mathbf{v}(0) = \mathbf{i} - \mathbf{j}$, $\mathbf{r}(0) = \mathbf{j}$

24. Section 13.4 #28.