

Name: \_\_\_\_\_

Math 162, Intro to Math Methods and Applications – Crawford

Exam 2 - Form A

09 November 2016

Score

1	/5
2	/10
3	/5
4	/10
5	/12
6	/12
7	/10
8	/12
9	/12
10	/5
11	/10
Total	/100

- You may use the given formula sheet. Books or other notes (in any form) are not allowed.
- You may use a calculator, but you must show work for credit.
- *Show all your work* – partial credit may be given for written work.
- Clearly indicate your answers.
- Good Luck!

Calculator Number:

1. (5 pts). Find the sum of the first 112 terms of an arithmetic sequence with first term 4 and common difference  $\frac{1}{2}$ .

2. (10 pts). Solve the following equations for  $x$ .

(a).  $6000 = 250(1.07)^x$

(b).  $\ln(2x - 1) - \ln 3 = \ln 9$

3. (5 pts). If \$1800 is invested for 6 months at an annual *simple* interest rate of 8%, what is the future value after 6 months?

4. (10 pts). What is the future value if \$10,000 is invested for 2 years at 5%

(a). Compounded quarterly?

(b). Compounded continuously?

5. (12 pts). An individual deposits \$150 at the end of each month into an account that earns 8.4%, compounded monthly.

(a). How much will be in the account at the end of 6 years?

(b). If the individual wants \$20,000 in the account at the end of 6 years, how big should the monthly payments be?

6. (12 pts). Develop an amortization schedule for a loan of \$30,000 with interest at 5.5%, compounded annually, if it is to be repaid in 3 years by making 3 annual payments of equal size.

Period	Payment	Interest	Balance Reduction	Unpaid Balance
	-	-	-	30000.00
1				
2				
3				

7. (10 pts). Find the following limits, if they exist. [Show work for credit.]

(a).  $\lim_{x \rightarrow -1} \frac{-3x + 3}{x^2 + 4}$

(b).  $\lim_{x \rightarrow 2} \frac{x^2 - 2x}{x^2 + 3x - 10}$

8. (12 pts). Given  $f(x) = 4 - 3x^2$ , **use the limit definition**  $\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ , to show that the derivative  $f'(x)$  is  $-6x$ . **To help with this process complete the following steps:**

(a). **Step 1.** Write down  $f(x)$ .

(b). **Step 2.** Find and simplify  $f(x+h)$ .

(c). **Step 3.** Find and simplify  $\frac{f(x+h) - f(x)}{h}$ . [Clearly show all algebraic steps.]

(d). **Step 4.** Take the limit as  $h \rightarrow 0$  of  $\frac{f(x+h) - f(x)}{h}$ .

For the remainder of the review sheet, use the DERIVATIVE FORMULAS, not the limit definition!

9. (12 pts). Given  $f(x) = 2x^4 - 3x^2 - 2x - 10$ ,

(a). Find the derivative of  $f(x)$ .

(b). Find the equation of the tangent line to  $f(x)$  at  $x = 2$ .

10. (5 pts). Find the derivative of  $g(x) = \frac{2}{x^3} + 4\sqrt{x}$

11. (10 pts). The profit function for producing  $x$  units is given by  $P(x) = 80x - 0.1x^2 - 7000$  in dollars. Find and interpret the marginal profit for  $x = 500$  units.