

1. Solve the following systems of linear equations algebraically. Show all your work. If the system is dependent or inconsistent, clearly state so.

$$(a). \begin{cases} -3x + 2y = -4 \\ 2x + 4y = 8 \end{cases} \quad x = 2, y = 1 \quad (b). \begin{cases} x - 3y = 5 \\ -3x + 9y = -10 \end{cases} \quad \text{Inconsistent; No Solution}$$

2. A movie theater charges \$9 for adults and \$5.50 for children. On the opening day for the latest Harry Potter movie, the theater fills all 500 of its seats. If they collected \$3870, how many children and how many adults watched the movie?

Set up, **but do not solve**, the system of equations needed to determine how many children and how many adults watched the movie. Clearly indicate what x and y represent.

$$\text{Let } x = \text{number of adults and } y = \text{number of children. Then } \begin{cases} x + y = 500 \\ 9x + 5.50y = 3870 \end{cases}$$

3. A manufacturer of DVD players has monthly fixed costs of \$9800 and variable costs of \$65 per unit for one particular model. The company sells this model to dealers for \$100 each.

(a). For this model DVD player, write the function for the monthly total costs, revenue, and profit.

$$C = 65x + 9800; R = 100x; P = 35x - 9800$$

(b). Find $R(250)$ and interpret the answer.

$$R(250) = 25000. \text{ The revenue from selling 250 units is } \$25,000.$$

(c). Find the marginal profit and write a sentence that explains its meaning. $\overline{MP} = 35$. Each additional unit sold will result in \$35 additional profit.

(d). Find the break-even point.

$$280 \text{ units}$$

4. Find the market equilibrium point for the following demand and supply functions.

$$(a). \text{ Demand: } p = 600 - 3q \quad \text{Supply: } p = 21q + 96 \quad p = 537, q = 21$$

$$(b). \text{ Demand: } p = 2q^2 + q + 40 \quad \text{Supply: } p = 200 - q - \frac{1}{4}q^2 \quad p = 176, q = 8$$

$$5. \text{ Solve the following equations for } x: \quad (a). x^2 - 6 = x + 6 \quad x = 4, -3 \quad (b). 3x^2 - 10x + 8 = 0 \quad x = 2, \frac{4}{3}$$

6. Given the parabola $y = -3x + x^2$ [Do this problem without a calculator.]

(a). Find the x and y coordinates of the vertex. $(\frac{3}{2}, -\frac{9}{4})$ (b). Is it a maximum or a minimum? min.

(c). Find the x - and y -intercepts x -int: (0,0) and (3,0), y -int: (0,0) (d). Sketch the graph and label 3 pts.

7. The percent of total work force that is female is given by $p(t) = -0.0034t^2 + 0.45t + 34$, where t is the number of years past 1970. In what year is the percent of females in the workforce a maximum? What is that maximum percentage? vertex at $t \approx 66.18$, so in the year 2036 (nearly 2037) and the maximum percent is 48.89%

8. The monthly charge for water in a small town is given by $f(x) = \begin{cases} 62 & \text{if } 0 \leq x \leq 25 \\ 62 + 0.5(x - 25) & \text{if } x > 25 \end{cases}$ where x is water usage in hundreds of gallons and $f(x)$ is in dollars.

(a). Find the monthly usage charge when the water usage is (i) 80 gallons (ii) 4000 gallons (i) \$62 (ii) \$69.50

(b). Graph the function for $0 \leq x \leq 100$.

9. Solve the following inequalities. Write your answers in interval notation and graph it on the number line.

$$(a). 2x + 1 > 4 \quad (\frac{3}{2}, \infty) \quad (b). 2(7x - 3) \leq 12x + 16 \quad (-\infty, 11]$$

$$10. \text{ Solve the following inequality. Graph the solution on the number line. } x^2 - x - 6 \leq 0 \quad [-2, 3]$$

11. Given the system of inequalities
$$\begin{cases} x + 4y \geq 10 \\ 2x + 6y \geq 18 \\ x \geq 0 \\ y \geq 0 \end{cases}$$

- (a). Shade the feasible region (b). Find the corners $(0, 3), (10, 0), (6, 1)$
 (c). Minimize $f = 3x + 2y$ subject to the same constraints Minimum of 6 at $(0, 3)$.

12. Solve the following inequalities. Graph the solution on the number line.

(a). $x^2 - x - 6 \leq 0$ $[-2, 3]$ (b). $\frac{(x-3)^2}{(x+1)(x+2)} \geq 0$ $(-\infty, -2) \cup (-1, \infty)$

13. (a). Write in exponential form: $\log_3 81 = 4$ $3^4 = 81$ (b). Write in logarithmic form: $8^{1/3} = 2$ $\log_8 2 = \frac{1}{3}$

14. Graph the following functions (without a calculator) and clearly label 2 points.

(a). $y = 2e^x$ (b). $y = 3^{-x}$ (c). $y = \log_4 x$

15. Use properties of logarithms to expand the following logarithms as far as you can.

(a). $\log_2 x^3 y^4 = 3 \log_2 x + 4 \log_2 y$ (b). $\log \frac{1}{\sqrt{A}} = -\frac{1}{2} \log A$ (c). $\log_b [P(1+r)^t] = \log_b P + t \log_b (1+r)$

16. Use properties of logarithms to combine the following into a single logarithm.

(a). $\log x^3 - 2 \log y = \log \frac{x^3}{y^2}$ (b). $\log_2(x-1) + \log_2(x+1) - \frac{1}{2} \log_2 x = \log_2 \frac{x^2 - 1}{\sqrt{x}}$

17. Use the change of base formula to rewrite and/or evaluate the following.

(a). $\log_7 21 = \frac{\ln 21}{\ln 7} = 1.5645$ OR $= \frac{\log 21}{\log 7} = 1.5645$ (b). $y = \log_2 x = \frac{\ln x}{\ln 2}$ OR $= \frac{\log x}{\log 2}$

18. Solve the following equations for x .

(a). $3^{5x} = 81$ $x = \frac{4}{5}$ (b). $\log_9 x = \frac{1}{2}$ $x = 3$

19. After an advertising campaign, the monthly sales for stereos at a store is given by $S = 50,000(2)^{-0.85x}$ S is the monthly sales (in dollars) and x is the number of months that have passed since the end of the advertising.

- (a). What is the monthly sales right at the end of the advertising? $S = 50,000(2)^{-0.85 \cdot 0} = \$50,000.00$
 (b). What is the monthly sales after 3 months? $S = 50,000(2)^{-0.85 \cdot 3} = \8537.75

20. An initial amount of 15 g of radioactive iodine decays according to $A(t) = 15e^{-0.087t}$ where t is given in days.

- (a). How much is left after 2 days? $A(2) = 12.6$ g