## Other Types of Indeterminate Forms

1. Quotients: So far we have primarily looked at InDETERMINATE FORMS that are quotients: $\frac{0}{0}, \frac{ \pm \infty}{ \pm \infty}$. Hence, the following quotients are Determinate Forms, meaning you know the limit. Indicate the following limits, for a constant $c \neq 0$ [Note: You may indicate $\pm \infty]$ :
(a). $\frac{c}{0} \rightarrow$
(b). $\frac{0}{c} \rightarrow$
(c). $\frac{ \pm \infty}{c} \rightarrow$
(d). $\frac{c}{ \pm \infty} \rightarrow$
2. Products. Only one of the following products gives an indeterminate form. Cirle this one and then state the value of the limit for the other four forms.

$$
\begin{array}{cccc}
c \cdot 0 & c \cdot \pm \infty & \infty \cdot \infty & -\infty \cdot \infty
\end{array}
$$

3. Sums and Differences. Only one of the following gives and indeterminate form. Circle this one and then state the value of the limit for the other two forms.

$$
-\infty-\infty \quad \infty-\infty \quad \infty+\infty
$$

4. Powers. Fill in the following blanks. The following two powers are Determinate Forms:

$$
0^{\infty} \quad 0^{-\infty}
$$

(a). Zero multiplied by itself over and over is still $\qquad$ . So in the limit $0^{\infty}$, we get $\qquad$ since it doesn't matter whether you approach zero from above or below, it still goes to zero.
(b). $0^{-\infty}=\frac{1}{0^{\infty}}=\frac{1}{0} \rightarrow$

The following three powers are Indeterminate Forms:

$$
0^{0} \quad \infty^{0} \quad 1^{\infty}
$$

(a). $0^{0}$ : Zero raised to any number "should" be $\qquad$ . But any number raised to zero "should" be
$\qquad$ . So $0^{0}$ is indeterminate because "reason" gives two competing answers.
(b). $\infty^{0}$ : Infinity (or a really big number) raised to a power "should" still be $\qquad$ , but any number raised to the zero "should" be $\qquad$ . So $\infty^{0}$ is indeterminate because "reason" gives two competing answers.
(c). $1^{\infty}: 1.00001$ multiplied by itself over and over will get larger. But 0.99999 multiplied by itself over and over will get $\qquad$ . So the limit $1^{\infty}$ is also an $\qquad$ form.
5. For each of the following limits, clearly state which indeterminate form is obtained. Then do"MORE WORK" (e.g., factor and cancel, limit at infinity shortcuts, etc.) to determine the limit.
(a). $\lim _{x \rightarrow 2} \frac{x^{2}-4}{x-2}$
(b). $\lim _{x \rightarrow \infty} \frac{5 x^{2}-1}{2 x^{2}-4}$
6. Answer the following questions about each limit.
(a). Observe that $\lim _{x \rightarrow \infty} \frac{\ln x}{x-1}$ results in the Indeterminate Form $\frac{\infty}{\infty}$

Do you think the top is going to infinity

> Faster, Slower, or At the Same Rate as the bottom? [Circle One]

Based on your answer do you think the limit will be
$\infty \quad 0 \quad$ or $\quad$ A Finite Nonzero Number? $\quad$ [Circle One]

Graph the function and see if you were correct about the limit.
(b). Observe that $\lim _{x \rightarrow \infty} \frac{1-e^{2 x}}{x^{2}}$ results in the Indeterminate Form $\frac{-\infty}{\infty}$

Do you think the top is going to negative infinity
Faster, Slower, or At the Same Rate as the bottom? [Circle One]
Based on your answer do you think the limit will be
$-\infty \quad 0 \quad$ or $\quad$ A Finite Nonzero Number? $\quad$ [Circle One]
Graph the function and see if you were correct about the limit.

