

1. Find the SUM of the following series or show that it diverges.

(a). $\sum_{n=1}^{\infty} \left(\frac{1}{n} + (-1)^n \right)$

(b). $\sum_{n=0}^{\infty} \frac{3^{n-1}}{5^{n+2}}$

(c). $\sum_{n=2}^{\infty} \left(\frac{1}{n-1} - \frac{1}{n+1} \right)$

(d). $\sum_{n=1}^{\infty} \frac{3^{2n}}{4^n}$

2. Given $\sum_{n=1}^{\infty} \frac{4}{n^3}$

(a). Find the 3rd partial sum s_3 .

(b). If s_3 is used to approximate the infinite series, what is the bound for the maximum possible error? (i.e. bound on $|R_3|$?)

(c). How many terms are needed for error to be less than 0.001.

3. Determine whether the following series converge or diverge. Show all your work and clearly indicate any tests that you use.

(a). $\sum_{n=1}^{\infty} \frac{5n^2 + n}{3 - 2n^2}$

(d). $\sum_{n=1}^{\infty} \frac{(n!)^2 3^n}{(2n)!}$

(b). $\sum_{n=1}^{\infty} \frac{5\sqrt{n} + 1}{3 + 2n^2}$

(e). $\sum_{n=1}^{\infty} \left(\frac{n}{2n-1} \right)^{3n}$

(c). $\sum_{n=1}^{\infty} \frac{\ln n}{n}$

(f). $\sum_{n=1}^{\infty} \frac{\cos n}{n^2}$

[More practice can be found in Section 11.7 and the Chapter 11 Review.]

4. Does $\sum_{n=2}^{\infty} (-1)^{n-1} \frac{1}{\ln n}$ converge absolutely, converge conditionally, or diverge.

5. Given $\sum_{n=0}^{\infty} (-1)^n \frac{1}{n+4}$

- (a). Find the 5th partial sum s_5 .
- (b). If s_5 is used to approximate the infinite series, what is the bound for the maximum possible error? (i.e. bound on $|R_5|$?)
- (c). How many terms are needed for error to be less than 0.001.

6. Find the interval and radius of convergence for the following series.

(a). $\sum_{n=1}^{\infty} \frac{3^n x^n}{n^n}$

(b). $\sum_{n=1}^{\infty} \frac{(-1)^n (x+2)^n}{n}$

(c). $\sum_{n=1}^{\infty} \frac{(2x+4)^n}{n4^n}$

7. Find the radius of convergence for the following series.

(a). $\sum_{n=0}^{\infty} \frac{(3x-2)^n}{n}$

(b). $\sum_{n=0}^{\infty} \frac{n^n x^n}{n!}$

8. Use a known power series to find a power series representation for the $f(x) = \frac{1}{1+3x^2}$.