

Use properties of logarithms to expand the following. Go as far as you can using the properties.

1.  $\log_3 \frac{x^5}{y^3}$

2.  $\log_b \sqrt[3]{N}$

3.  $\log(3^2 \sqrt[3]{4})$

4.  $\log_2(50 \cdot 2^{-0.2t})$

5.  $\ln[P(1+r)^t]$

6.  $\log_{\frac{1}{2}} \frac{\sqrt{a}}{b^3}$

Combine the following into a single logarithm of the form  $\log_b[ \ ]$ . Simplify as much as possible.

7.  $2 \ln x - 3 \ln(x+1)$

8.  $\log_4 x + \frac{2}{3} \log_4(x+5)$

9.  $\frac{1}{2} \log_2 9 - \log_2 6$

10.  $\frac{1}{2} \log 4 - \frac{2}{3} \log 8 + 2 \log 2$

Use properties of logarithms to combine the LHS and find  $x$ . [Be sure to check your answer in the original equation.]

**11.**  $\log x + \log 4 = \log 20$

**12.**  $\log_8(x + 2) + \log_8 x = \log_8 24$

Use the change of base formula to find the following.

**13.**  $\log_5 18$

**14.**  $\log_4(.14)$

Use the change of base formula and your calculator to graph the following. [Copy the graph below and label the axes.]

**15.**  $y = \log_7 x$

**1.**  $5 \log_3 x - 3 \log_3 y$

**2.**  $\frac{1}{3} \log_b N$

**3.**  $2 \log 3 + \frac{1}{3} \log 4$

**4.**  $\log_2(50) - 0.2t$

**5.**  $\ln P + t \ln(1 + r)$

**6.**  $\frac{1}{2} \log_{\frac{1}{2}} a - 3 \log_{\frac{1}{2}} b$

**7.**  $\ln \left( \frac{x^2}{(x+1)^3} \right)$

**8.**  $\log_4 \left( x \sqrt[3]{(x+5)^2} \right)$

**9.**  $-1$

**10.**  $\log 2$

**11.**  $x = 5$

**12.**  $x = 4$

**13.**  $1.79588$

**14.**  $-1.41825$

**15.** calculator